Space-to-Ground Quantum Key Distribution Using a Small-Sized Payload on Tiangong-2 Space Lab *

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Quantum technology establishes a foundation for secure communication via quantum key distribution (QKD). In the last two decades, the rapid development of QKD makes a global quantum communication network feasible. In order to construct this network, it is economical to consider small-sized and low-cost QKD payloads, which can be assembled on satellites with different sizes, such as space stations. Here we report an experimental demonstration of space-to-ground QKD using a small-sized payload, from Tiangong-2 space lab to Nanshan ground station. The 57.9-kg payload integrates a tracking system, a QKD transmitter along with modules for synchronization, and a laser communication transmitter. In the space lab, a $50\,\mathrm{MHz}$ vacuum + weak decoy-state optical source is sent through a reflective telescope with an aperture of $200\,\mathrm{mm}$. On the ground station, a telescope with an aperture of $1200\,\mathrm{mm}$ collects the signal photons. A stable and high-transmittance communication channel is set up with a high-precision bidirectional tracking system, a polarization compensation module, and a synchronization system. When the quantum link is successfully established, we obtain a key rate over $100\,\mathrm{bps}$ with a communication distance up to $719\,\mathrm{km}$. Together with our recent development of QKD in daylight, the present demonstration paves the way towards a practical satellite-constellation-based global quantum secure network with small-sized QKD payloads.

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Secure key distribution is one of the fundamental tasks in information science and technology. For example, the one-time pad encryption, [1] whose security is proven by Shannon, [2] requires an efficient way of secure key distribution. The principles of quantum mechanics can make two remote users, Alice and Bob, share identical private keys. Since the first quantum key distribution (QKD) protocol, the Bennett-Brassard-1984 (BB84)[3] protocol, tremendous developments have been made to bring the theory to reality. The ultimate goal is to establish a global quantum network or a secure quantum wide-area network.

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The first QKD experiment was implemented in 1989 with a communication distance of $32\,\mathrm{cm}$. [4] Then the distance is extended to kilometers, [5] dozens of kilometers, [6] and up to $100\,\mathrm{km}$ [7,8] in free space, and up to several hundreds of kilometers [9–13] in fiber. Meanwhile, urban quantum networks have been demonstrated in telecom network around the world. [14–16]

For both fiber and free space channels, practical QKD faces a key challenge that quantum signals cannot be amplified. This restricts the transmission distance of the scheme due to the increasing level of the

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attenuation and noise. For instance, with a 10 GHz perfect single-photon source and prefect detectors, it takes 300 years to transmit one bit for a distance of 1000 km in the standard telecom fiber.

To realize long distance quantum communication for a global quantum network, two promising methods have been proposed to relay signals: one is the quantum repeater scheme^[17] and the other is the satellite scheme.^[18] The repeater scheme requires high-performance quantum memory devices, which are not available with the current technology. The satellite-based scheme is much more practical due to the advantage of little attenuation of light in space, where photons can travel from satellites to ground stations through thousands of kilometers. Moreover, the satel-

lite can share keys with different ground stations globally due to the orbital motion. In recent years, great efforts have been made to test the feasibility of the satellite-to-ground QKD, including moving platforms^[8,19] and long-distance free space channel on the ground.^[7,8]

The quantum science experiment satellite Micius was launched on 16th August 2016. After several months' testing and experiment, satellite-based entanglement distribution over 1200 kilometers, $^{[20]}$ satellite-to-ground QKD $^{[21]}$ and ground-to-satellite quantum teleportation $^{[22]}$ have been demonstrated. These results pave the way to global-scale quantum networks and space-scale quantum experiments.

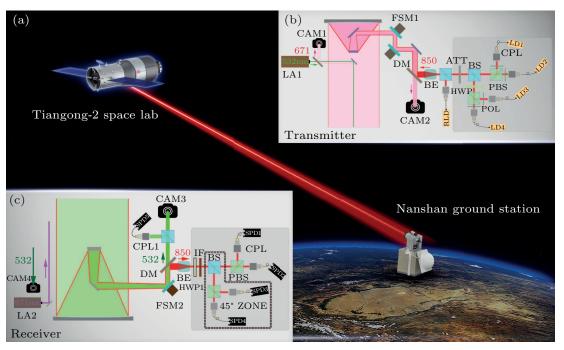


Fig. 1. Schematic diagram of the experimental setup. (a) Overview of the space-to-ground QKD. (b) Schematic of the decoy-state QKD transmitter. (c) Schematic of the decoy-state QKD decoder in the Nanshan ground station equipped with a 1200-mm-aperture telescope. LA1: green laser (532 nm), CAM1: coarse camera, CAM2: fine camera, LD: laser diode, RLD: reference laser diode, FSM1: fast steering mirror, HWP: half-wave plate, POL: polarizer, PBS: polarization beam splitter, BS: beam splitter, ATT: attenuation, LA2: red laser (671 nm), CAM3: fine camera, CAM4, coarse camera, CPL: coupler, DM: dichroic mirror, IF: interference filter, FSM2: fast steering mirror, BE: beam expander, SPD: single photon detector.

On the other hand, small-sized payloads for QKD, which can be assembled on either small satellites or big satellites such as space stations, can reduce the cost to construct a satellite constellation. Therefore, demonstrating the feasibility of QKD using small-sized and low-cost payloads is an important task. In this Letter, we report a space-to-ground QKD experiment using a small payload between the Tiangong-2 space lab and the Nanshan ground station (43°28′31.66″N, 87°10′36″E). The payload is 57.9 kg weight and integrates a tracking system, a QKD transmitter along with modules for synchronization, and a laser communication transmitter. The scheme is illustrated in

Fig. 1. The transmitter (Alice) is put in the Tiangong-2 space lab and the receiver (Bob) is put in the Nanshan ground station. The BB84 QKD protocol is implemented with the vacuum+weak decoystate scheme. $^{[23,24]}$ The experimental system includes a high-speed decoy-state source, a low beam diffraction optical system, a high-precision bidirectional tracking system, a polarization compensation module, and a synchronization system. In the experiment, the communication distance is within the range between 388 km and 719 km, the quantum bit error rate (QBER) is 1.8% and the final key rate is about 91 bps when the quantum channel is established.

A schematic diagram of the transmitter in the space lab is shown in Fig. 1(b). Based on the decoystate BB84 protocol, the source is made up with four vertical cavity surface emitting lasers and a BB84 encoding module. Photons are sent through a 200 mm diameter telescope to get a narrow divergence angle. A green laser beam which has a wavelength 532 nm, a power of 160 mW, a divergence angle of 1.25 mrad, a pulse full width at half maximum of 1.4 ns, and a repetition rate around 10 kHz, is coaxial with the telescope for system tracking and synchronization. In addition, there is a reference laser used for monitoring the channel depolarization.

The quantum source emits vacuum decoy states, weak decoy states, and signal states for the vacuum+weak decoy-state BB84 scheme. The average photon number of the weak decoy state is $\nu = 0.35$, and that of the signal state is $\mu = 0.6$. Each of the decoy/signal state is randomly prepared in one of the four BB84 states, $|H\rangle$, $|V\rangle$, $|+\rangle$ and $|-\rangle$, where $|H\rangle$ and $|V\rangle$ represent the horizontal and vertical polarizations, respectively, and $|\pm\rangle = (|H\rangle \pm |V\rangle)/\sqrt{2}$ represent diagonal polarizations. Four fiber-coupled laser diodes with a wavelength of 850.15 nm, a repetition rate of 50 MHz, and a full width at half maximum of around 500 ps, are employed to emit photons in four paths for the BB84 encoding. The encoding module includes a half-wave plate (HWP), a beam splitter (BS), and two polarization beam splitters (PBSs). After encoding, a passive attenuator is employed to set the average photon number per pulse to the designed quantum level when the pulses leave the transmitter telescope. The intensity of each laser diode is randomly modulated to prepare the signal states, weak decoy states, and vacuum decoy states, whose ratio is set to 2:1:1. The random numbers used for state preparation are generated beforehand by a random physical noise chip.

From the security point of view, it is critical to make photons indistinguishable from the four lasers in both of the spectrum and the temporal domains. The wavelengths of the laser diodes are carefully tuned to 850.15 nm by separate temperature controllers. The centers of the optical pulses are precisely controlled by adjusting the length of the driver's cable. The output beam is carefully aligned to the polarization encoding module with collimators to obtain both concentricity and coaxiality.

In the space-to-ground QKD experiment, the light sent from the space lab is at the single-photon level and needs to travel for hundreds of kilometers to reach the ground station. Therefore, the link transmission efficiency becomes critical. The geometric loss dominans the total attenuation. Since the link transmittance is inversely proportional to the square of the product of the beam divergence and the travel distance, it is important to narrow the QKD light beam. In the transmitter, we use a reflective telescope with

an aperture of 200 mm to narrow the beam divergence down to ${\sim}35\,\mu\mathrm{rad}$. The beam diameter is around 24.5 m after transmitting through 700 km free space. When a 1.2 m aperture telescope is used to collect the light, the corresponding geometric loss is about 27 dB.

The setup on the receiver's side is presented in Fig. 1(c). A Ritchey-Chretien telescope with aperture of 1.2 m and a focal length of around 10 m is used to collect the QKD photons. The received photons first go through a motorized HWP for dynamical polarization compensation, and an interference filter for suppressing background noises, then they are sent to the BB84 decoding module with four singlephoton detectors. The output electrical signals from the detectors are fed into a data acquisition computer with a time to digital convertor (TDC). The acquired data is stored in a harddisk for further processing. Meanwhile, a 671 nm continuous-wave red laser with a power of 2.2 W and a divergence angle of 1.2 mrad is sent from the ground station to the space lab for system tracking.

The relative rotation between the transmitter and the receiver effectively introduces a rotation of the photon polarization. Since the QKD setup uses polarization encoding, such rotation needs to be compensated for. We first evaluate the rotation angle by taking account of the relative rotations and all birefringent elements in the optical link, then we use a motorized HWP for the dynamical compensation.

As the Tiangong-2 space lab circles the earth with a speed of about $7.7\,\mathrm{km/s}$ and the beam divergence is only 35 μ rad, a high-precision acquisition, tracking and pointing (ATP) system^[25] becomes an essential component to establish the link between the space lab and the ground station. Both the transmitter and the receiver have a two-stage ATP system, which has a coarse tracking loop and a fine tracking loop.

The coarse tracking loop includes a two-axis gimbal and a camera with wide field-of-view and low frame rate. In the transmitter, a complementary metal oxide semiconductor (CMOS) camera is used and in the receiver a charge-coupled device (CCD) camera is used. The fine tracking loop includes a fast steering mirror (FSM) and a camera with narrow field-of-view and high frame rate. In the transmitter, a CMOS camera is used and in the receiver a CCD camera is used.

In the ATP system, first the receiver sends the 671 nm beacon laser to the transmitter. The transmitter captures the beacon laser with the coarse CMOS camera. Then the two-axis gimbal corrects its pointing direction according to the position of the light spot in the coarse camera, and guides the beacon laser into the fine CMOS camera. The FSM corrects its pointing direction according to the position of the light spot in the fine camera. The final tracking precision is about $1{\text -}2\,\mu\text{rad}$ during the experiment. In order to further increase the pointing precision from the ground station

to the space lab, the transmitter points the 532 nm beacon laser to the receiver. On the ground station, a beam splitter divides the received 532 nm light into two parts for tracking and synchronization, respectively. One part is used to guide the light into the detectors with a precision of 1–2 μrad . Then the stable optical link is established and remains locked in the closed-loop tracking. Note that the transmitter sends the QKD photons with a so-called point ahead angle, which is to compensate for the relative motion of the two terminals.

The other part of the 532 nm light is used for synchronization. The transmitter in the space lab sends 50 MHz light pulses as quantum signals to the receiver while most of these signals are lost in the channel. The timing of the detected signals on the receiver side needs to match the pulse indexes of the corresponding encoded signals on the transmitter side. Since the transmitter and the receiver are separated far away and have independent reference clocks, a high-precision synchronization is needed. The synchronization is also used to distinguish the QKD signal photons from background noises.

In the space lab, a small part of the 532 nm laser beam is used for synchronization, along with the Global Positioning System (GPS). The light is guided into a fast photodiode to be converted into electrical pulse signals. Meanwhile, a GPS receiver in the space lab emits pulse-per-second (PPS) signals. Both the pulse signals and the GPS PPS signals are fed into a TDC module of the transmitter. The TDC module uses the common clock with the QKD source encoding module. On the ground station, a part of the received 532 nm beacon is sent to a single-photon detector. The detection results, together with the GPS PPS signals, are used for the time reference of the quantum signal detections. As a result, the time jitter of the reference reaches 0.95 ns, which is used to tag the QKD detection events within a 2 ns time window in order to filter out background noises.

Table 1. Experimental procedures in different locations of the space lab and rough operation time.

Zenith angle	Main procedure	Time
of a typical pass		
Beneath horizon	System initialization	_
Horizon to 65°	Orientation initialization	$\sim 200 \mathrm{s}$
65° to 60°	ATP	$\sim 15 \mathrm{s}$
65° to 55°	Stable quantum link settlement	$\sim 27 \mathrm{s}$
55° to -65°	Quantum communication	~130 s
Beneath -65°	Data processing	_

The experimental procedures are listed in Table 1. The QKD link can be established only under the following conditions: (1) good weather and clear visibility; (2) the space lab and the ground station are in the shadow of the earth, that is, the experiment operates at night; (3) the duration when the transmitter on the space lab and the ground station can see each other is more than 60 s. When the space lab comes out

from the horizon, the receiver telescope is pointed to a predicted orbital position. Then the receiver turns on the beacon laser to cover the predicted area. The telescope in the space lab is also pointed to the ground station with a predicted direction. Once the transmitter captures the beacon laser from the ground station with the coarse camera, they start the ATP and establish a quantum link.

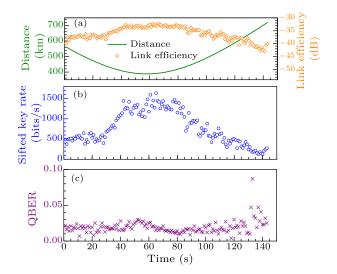


Fig. 2. Experimental results for one pass of space lab. (a) The distance of the space lab and the ground station and the link efficiency as a function of time. (b) The sifted key rate as a function of time. (c) Observed quantum bit error rate as a function of time.

On a typical orbit pass after the quantum link is established, the overall transmittance is nearly from $-32\,\mathrm{dB}$ to $-42\,\mathrm{dB}$ at the distance from $388\,\mathrm{km}$ to 719 km, which mainly includes the 21–26 dB geometric loss, the $-7 \, dB$ optical efficiency on the receiver side. On the detection side, the background count rate is around 300 cps, including the dark count rate of the four single-photon detectors. The signal count rate is around 1000–5000 cps. With the time filtering of 2 ns, we achieve a mean sifted key rate of 783 bps in 143 s and a QBER of 1.8%. In total, we obtain 112031 bits sifted key of signal. When the space lab passes over the ground station, the optical link distance and the channel transmittance vary with time, then the sifted key rate and the QBER change over time as well. We show the experimental results for one pass of the space lab in Fig. 2. One can see the inverse proportional relation between the distance and the transmittance. The QBER is relatively stable over time.

Meanwhile, we compare the performance of our space-based QKD with that expected from the conventional method using telecommunication fibers. At 719 km, the space-based QKD demonstrates a channel efficiency which is ~10 orders of magnitudes higher than that using the optical fiber with 0.2 dB/km loss.

In data post-processing, we apply the standard decoy-state QKD analysis. The key rate formula is

given by [23]

$$R_{\text{pulse}} \ge Q_1[1 - h(e_1)] - I_{\text{ec}},$$
 (1)

where $h(x) = -x \log_2 x - (1-x) \log_2 (1-x)$ is the Shannon binary entropy function, Q_1 is single-photon ratio of sifted key in the signal state, and e_1 is its phase error rate. The first term $Q_1[1-h(e_1)]$ represents the privacy amplification term. The second term $I_{\rm ec} = fQ_\mu h(E_\mu)$ denotes the secure key cost in error correction and f is the error correction inefficiency factor, which is typically a function of the QBER E_μ . In this work, we adopt a low-density-parity-check code. [26]

The values of Q_1 and e_1 can be estimated by the decoy-state method. We follow the recent work^[27] for the statistical fluctuation analysis of the vacuum+weak decoy-state QKD scheme. The cost in error correction is 16736 bits, which corresponds to $I_{\rm ec} = 4.68 \times 10^{-6}$. The privacy amplification ratio is $1 - h(e_1) = 0.75$. In our security analysis, the failure probability of each step is 10^{-5} . Finally, we obtain a 13,119 bit secure key, corresponding to the secure key rate of 91 bps.

In summary, we have demonstrated decoy-state QKD from a small-sized payload on Tiangong-2 space lab to Nanshan ground station with polarization encoding. In the experiment, the communication distance is within the range between 388 km and 719 km, the QBER is 1.8% and the average final key rate is around 91 bps. This kind of compact and low-cost payload used in the experiment can be assembled on satellites with various sizes to construct a satelliteconstellation-based quantum network. The performance of QKD and the size of the payload still have rooms to improve, e.g., reducing the size of the telescope to $\sim 100 \,\mathrm{mm}$, narrowing the divergence angle of the source to the diffraction limit, increasing the decoy-state source rate to 1 GHz. With such improvements, we can expect a payload with a weight of less than 20 kg, which can be assembled on a microsatellite to achieve a final key rate of around 10 kbps. When combining with daytime QKD technologies,^[28] designing the microsatellite, pointing a telescope to the ground station with precise better than 0.5° like Micius satellite, [21] the two-axis gimbal of the ATP system can be eliminated, and the weight of the whole satellite can be reduced below 100 kg. Then it would be a practical and low-cost solution to a quantum network based on microsatellite constellations.

Appendix A: data analysis

In data postprocessing, we apply the standard decoy-state QKD analysis to estimate the values of Q_1 and e_1 . The key rate formula was given in Ref. [29] and the statistical fluctuation analysis [27] is used. In this section, we show how to calculate the Z basis key rate R^z . The X basis key rate R^x could be calculate with same means. Then the total key rate R_{pulse} is

equal to $R^x + R^z$.

$$R^z \ge Q_1^z [1 - h(e_1^z)] - I_{\text{ec}}^z,$$
 (2)

$$Y_1^z \ge Y_1^{\mathrm{zL}} = \frac{\mu}{\mu\nu - \nu^2} \Big(Q_{\nu}^{\mathrm{zL}} e^{\nu} - \frac{\nu^2}{\mu^2} Q_{\mu}^{\mathrm{zU}} e^{\mu} - \frac{\mu^2 - \nu^2}{\mu^2} Y_0^U \Big), \tag{3}$$

$$Q_1^z \ge Q_1^{zL} = Y_1^{zL} e^{-\mu} \mu,$$
 (4)

$$e_1^{\text{pz}} \le e_1^{\text{bxU}} + \theta_x^U, \tag{5}$$

$$e_1^{\text{bx}} \le e_1^{\text{bxU}} = \frac{(E_{\nu} Q_{\nu}^x)^U e^{\nu} - 0.5 Y_0^L}{\nu Y_1^{\text{xL}}}.$$
 (6)

Then, we apply the statistical fluctuation analysis method in Ref. [27] as follows. When the failure probability is 10^{-5} , the number of standard deviations is roughly equal to 5.

$$Q_{\nu}^{\rm zL} = Q_{\nu}^{z} (1 - \frac{5}{\sqrt{Ns_{\nu}^{z}}}),$$
 (7)

$$Q_{\mu}^{\text{zU}} = Q_{\mu}^{z} \left(1 + \frac{5}{\sqrt{Ns_{\mu}^{z}}}\right),$$
 (8)

$$Y_0^L = Y_0(1 - \frac{5}{\sqrt{N_0 Y_0}}),\tag{9}$$

$$Y_0^U = Y_0(1 + \frac{5}{\sqrt{N_0 Y_0}}),\tag{10}$$

$$EQ_{\nu}^{\text{xU}} = EQ_{\nu}^{x} (1 + \frac{5}{\sqrt{NE_{\nu}^{x}}}),$$
 (11)

where the superscript x (or z) represents to the data on the x (or z) base, the data without superscript is on both the bases. Q^z_μ and Q^z_ν are the gains for the Z basis signal states and weak decoy states, respectively, Y_0 is the measured counting rate for vacuum decoy states, Ns^z_μ and Ns^z_ν are the numbers of the Z basis sifted key used as signal states, weak decoy states, N_0 is the number of vacuum decoy states, NE^x_ν is the error number of the X basis weak decoy states, EQ^x_ν is the error gain for the X basis sifted weak decoy states. The results are listed in Table 2.

In Eq. (5), $e_1^{\rm pz}$ is equal to the $e^{\rm bx}$ in the infinite key length case. However, there is a gap θ_x between them in the finite key length case. The gap θ_x could be estimated by the random sampling method^[30] as shown in Appendix B.

Table 2. Experimental parameters and results. T is the effective time for QKD, Q_{μ} and Q_{ν} are the gains for the sifted signal states and the sifted decoy states, respectively; Y_0 is the yield for the vacuum states, E_{μ} is the QBER of the signal states, R_{total} is the total final key size of the experiment, and R_{pulse} is final key rate per clock cycle.

T	Q_{μ}	Q_{ν}	Y_0
143 s	3.13×10^{-5}	1.88×10^{-5}	8.33×10^{-7}
E_{μ}	E_{ν}	$R_{ m total}$	$R_{\rm pulse}$
1.84%	2.14%	13119 bits	1.83×10^{-6}

Appendix B: Random sampling

In this section, we show how to estimate θ_x in Eq. (5) using the random sampling method. [30] Given e_1^{bx} , n_x (the number of the X basis single photon

state), and n_z (the number of the Z basis single photon state), we can bound $e_1^{\rm pz}$ with a small probability $\xi = 10^{-5}$.

$$\xi \equiv Pr\{e_1^{\text{pz}} \ge e_1^{\text{bx}} + \theta_x\},\tag{12}$$

Then we have

$$\xi < \frac{\sqrt{n_x + n_z}}{\sqrt{e_1^{\text{bx}} (1 - e_1^{\text{bx}}) n_x n_z}} 2^{-(n_x + n_z) \xi_x(\theta_x)}, \tag{13}$$

where $\xi_x(\theta_x)$ is given by

$$\xi_x(\theta_x) \equiv H(e_{\text{bx}} + \theta_x - q_x \theta_x) - q_x H(e_1^{\text{bx}}) - (1 - q_x) H(e_1^{\text{bx}} + \theta_x), \tag{14}$$

and $q_x = n_x/(n_x + n_z)$. We could find a root θ_x^U of Eq. (14) and know that

$$e_1^{\text{pz}} \le e_1^{\text{bx}} + \theta_x^U. \tag{15}$$

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