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Operational effects of the UNOT gate on classical and quantum correlations

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ABSTRACT

The NOT gate that flips a classical bit is ubiquitous in classical information processing. However its quantum analogue, the universal NOT (UNOT) gate that flips a quantum spin in any alignment into its antipodal counterpart is strictly forbidden. Here we explore the connection between this discrepancy and how UNOT gates affect classical and quantum correlations. We show that while a UNOT gate always preserves classical correlations between two spins, it can non-locally increase or decrease their shared discord in ways that allow violation of the data processing inequality. We experimentally illustrate this using a multi-level trapped $^{171}\text{Yb}^+$ ion that allows simulation of anti-unitary operations.

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1. Introduction

When given a quantum spin pointing in some unknown direction \vec{n} , is it possible to engineer a universal device that flips this spin to point in the antipodal direction $-\vec{n}$? While this process is easy to envision for classical vectors, it is strictly impossible for quantum spins. The quantum operation that takes an arbitrary quantum state $|\varphi\rangle$ to its orthogonal complement $|\varphi^\perp\rangle$ is anti-unitary, and thus does not exist [1–4]. Like the no-cloning theorem, this uniquely quantum constraint has drawn significant scientific interest [5–7].

In contrast to cloning, the radical operational consequences of the UNOT gate are not as readily apparent on a single qubit. Suppose Alice secretly encodes a direction \vec{n} in 3-dimensional space by preparing a spin aligned in \vec{n} . She then challenges Bob to estimate \vec{n} . If Bob can perfectly clone quantum states, then he can violate the uncertainty principle by measuring each clone in a different complementary basis. On the other hand, any measure-

ment Bob makes after applying a UNOT gate on the input spin can be simulated by measuring the input directly and reinterpreting the measurement outcome (recording “up” as “down” and vice versa). Thus UNOT gates do not allow Bob to retrieve information about \vec{n} beyond standard quantum limits.

The consequences of the UNOT gate surface when an ancillary qubit is introduced. Consider the same game, but now played on two qubits. Instead of sending a single spin, Alice now sends a pair of spins. Take two different strategies, either (1) sending Bob two aligned spins, both in direction \vec{n} , or (2) an anti-aligned pair, with one spin in direction \vec{n} , and the other in direction $-\vec{n}$. Gisin and Popescu [1] illustrated that the second strategy improves Bob's capacity to estimate \vec{n} . They noted that if Bob possesses a UNOT gate, he can deterministically convert a pair of aligned spins to anti-aligned spins, and thus break standard quantum limits whenever Alice adopts strategy (1).

This connection suggests that UNOT gate exhibits distinctive effects on quantum correlations. Here we formalize this intuition using recent methods that isolate the purely quantum component of correlations between two systems. These correlations, known as discord, are often motivated as correlations accessible only to quantum observers [8–10]. We show that the UNOT gate preserves

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classical correlations between two spins, but can change their shared quantum correlations in ways forbidden by fundamental data processing principles (Fig. 1a). We illustrate this through experiment – by adapting recent ion trap technology that allows perfect simulation of anti-unitary operations [11–13]. We then outline how these results rationalize the discrepancy in communication rate between aligned and anti-aligned spins, showing that it exactly relates to the UNOT gate's non-trivial effect on discord during the decoding process.

2. Theory

2.1. Technical framework

Consider first two classical spins A and B. Let $S(\cdot)$ denote the information entropy function, such that $S(A)$ and $S(B)$ quantify the respective uncertainties of A and B when viewed independently and $S(AB)$ the uncertainty of the joint spin pair. The mutual information $I(A, B) = S(A) + S(B) - S(AB)$ then captures the total correlations between A and B. This coincides with

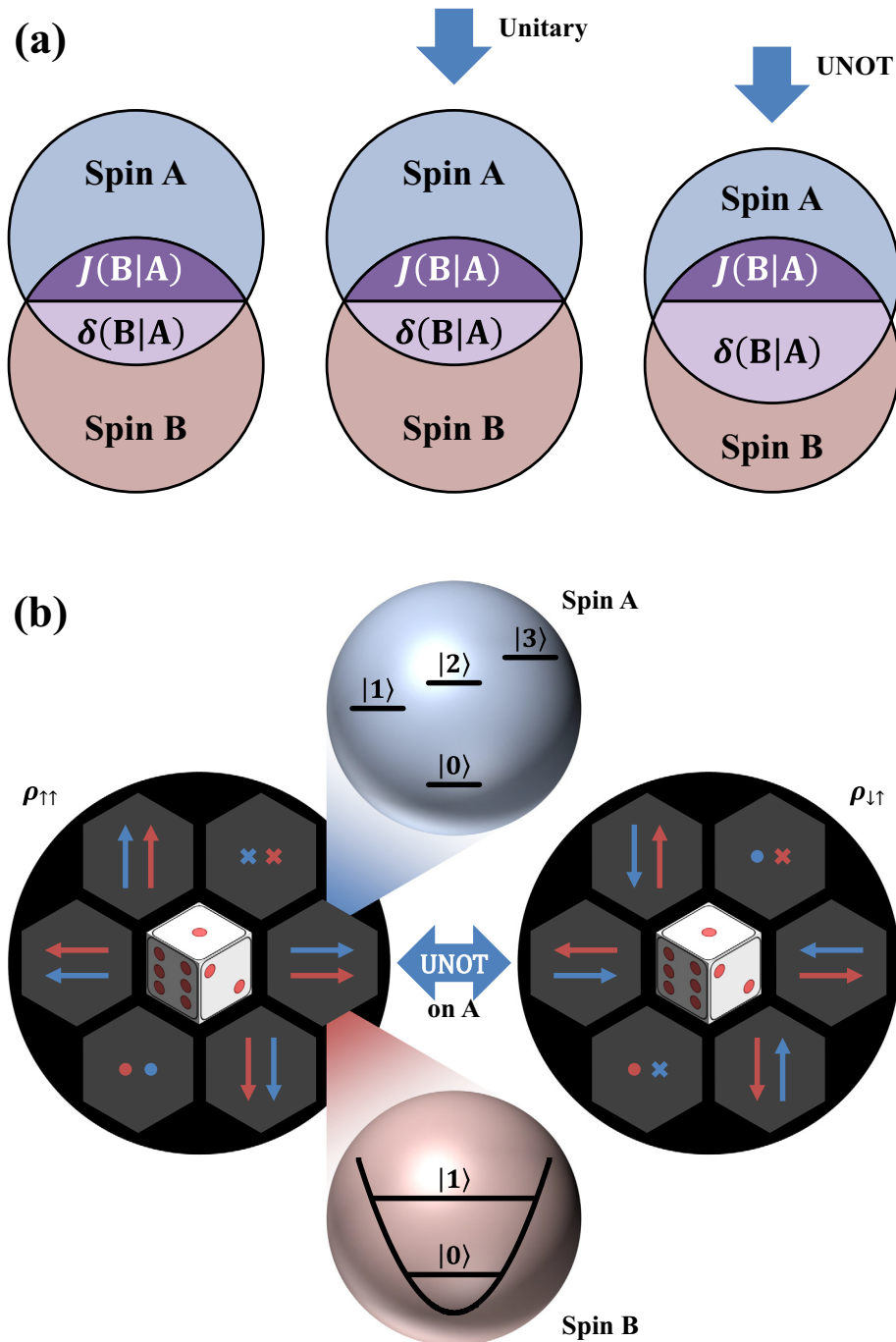


Fig. 1. UNOT gates on spin pairs. (a) Local reversible operations leave classical correlations $J(B|A)$ and quantum correlations $\delta(B|A)$ unchanged, where A and B are two separable spins. A UNOT gate also preserves $J(B|A)$, but can change $\delta(B|A)$. (b) We simulate the effect of UNOT on $\rho_{\uparrow\uparrow}$ and $\rho_{\downarrow\uparrow}$, where the two spins are encoded in the internal and external degrees of freedom of a trapped $^{171}\text{Yb}^+$ ion in a harmonic potential. Spin A is mapped to a 4-level system using Eq. (1), spanned by the basis $|0\rangle_A = |F=0, m_F=0\rangle$ and $|n=1, 2, 3\rangle = |F=1, m_F=n-2\rangle$, where F and m_F characterize the total internal angular momentum of $^{171}\text{Yb}^+$. The transition frequency from $|F=0, m_F=0\rangle$ to $|F=1, m_F\rangle$ is $(2\pi)(12642.8 + 9.0m_F)$ MHz. Spin B is mapped to the ground and first excited states of external motional mode, denoted by $|0\rangle_B$ and $|1\rangle_B$, which are separated by the trap frequency $(2\pi)2.44$ MHz.

$J(B|A) = S(B) - S(B|A)$, the reduction of uncertainty in B, when someone measures and communicates the state of A. The data processing inequality implies that $I(A, B)$ can never increase under local operations [14,15]. This reflects the principle that we can never spontaneously obtain more information about a spatially separated system B through local operations on A. Consequently, any reversible operation on A must conserve $I(A, B)$ – a condition clearly satisfied by the classical NOT gate.

When the two spins are quantum, the analogues of $I(A, B)$ and $J(B|A)$ no longer coincide. Any positive operator valued measurements (POVMs) $\{\Pi_a\}$ on A can induce unavoidable noise, limiting the entropy reduction on B to $J(B|A) = \sup_{\{\Pi_a\}} [S(B) - \sum_a p_a S(B|a)]$, where p_a is the probability of getting outcome a , and $S(B|a)$ represents the corresponding entropy of B conditioned on this outcome. In literature, $J(B|A)$ is considered to be the classical component of $I(A, B)$, as it represents how much information a classical observer can gain about B when measuring A. The remaining portion, $\delta(B|A) = I(A, B) - J(B|A)$, is defined as the quantum discord, and interpreted as the purely quantum correlations between A and B [8,10,16–18].

2.2. Theoretical results

Let ρ be a separable bipartite state on two spins, A and B. Here we establish the following relations between the UNOT gate and classical and quantum correlations:

- (i) Local UNOT gates preserve $J(B|A)$ and $J(A|B)$.
- (ii) If $\delta(B|A) = 0$, a local UNOT gate conserves $I(A, B)$.
- (iii) Local UNOT gates can nevertheless violate the data processing inequality, but only when $\delta(B|A) > 0$.

Result (i) implies that the UNOT gate can never break the data processing inequality for classical correlations. A classical observer that quantifies correlations by local measurement (i.e., $J(A|B)$ or $J(B|A)$) will conclude that the UNOT gate has no radical effects. Meanwhile result (ii) implies that the UNOT gate always obeys the data processing inequality, provided no discord is present. Finally result (iii) shows that the UNOT gate can violate the data processing inequality, but only when discord is present. Furthermore, this violation can only be witnessed when purely quantum correlations are taken into account. Proofs for (i) and (ii) are given in the [Supplementary data](#), while we demonstrate (iii) directly by explicit examples.

3. Experiment

3.1. Protocol

Our experiment considers a separable bipartite quantum state $\rho_{\uparrow\uparrow}$ constructed as follows: first let $\mathcal{I} = \{\vec{x}, -\vec{x}, \vec{y}, -\vec{y}, \vec{z}, -\vec{z}\}$ represent a set of six standard coordinate directions in 3-dimensional space. We select a direction $\vec{n} \in \mathcal{I}$ uniformly at random, and prepare one spin aligned in direction $-\vec{n}$ and the other in \vec{n} . Denote their states respectively by $|-\vec{n}\rangle_A$ and $|\vec{n}\rangle_B$. The choice of \vec{n} is then discarded. The resulting mixed state $\rho_{\uparrow\uparrow} = \sum_{\vec{n} \in \mathcal{I}} |-\vec{n}\rangle_A \langle -\vec{n}|_A \otimes |\vec{n}\rangle_B \langle \vec{n}|_B / 6$ then describes two anti-aligned spins that are oriented along one of the six directions in \mathcal{I} at random. Application of the UNOT gate on one of the two spins then results in the state $\rho_{\uparrow\uparrow} = \sum_{\vec{n} \in \mathcal{I}} |\vec{n}\rangle_A \langle \vec{n}|_A \otimes |\vec{n}\rangle_B \langle \vec{n}|_B / 6$ which represents two aligned spins oriented randomly in some direction $\vec{n} \in \mathcal{I}$ (Fig. 1b). By result (i), $\rho_{\uparrow\uparrow}$ and $\rho_{\uparrow\uparrow}$ must have coinciding classical correlations $J(B|A)$.

Here we conduct two separate experiments. In the first, we prepare $\rho_{\uparrow\uparrow}$ on a spin pair, and simulate the action of the UNOT gate on one of the two spins. We characterize, by tomography, the effect of this action on the classical and quantum correlations within the spin pair. This process is then repeated with $\rho_{\uparrow\uparrow}$ in place of $\rho_{\uparrow\uparrow}$. This allows us to experimentally demonstrate result (iii) by showing that the local application of a UNOT gate can fundamentally increase or decrease $\delta(B|A)$ while preserving $J(B|A)$, and thus violate the data processing inequality.

3.2. Simulating UNOT

The experiment involves exact simulation of the UNOT gate – an unphysical operation. Indeed, all existing demonstrations of the UNOT gate are based on theoretically optimal approximations [5,6]. We circumvent these issues by embedding the state of spin A within a larger Hilbert space (see Fig. 2 – a technique recently proposed for exactly simulating anti-unitary operations [12,13]). This approach maps each spin state $|\varphi\rangle = \alpha|\uparrow\rangle + \beta|\downarrow\rangle$ to a corresponding state

$$\mathcal{M}|\varphi\rangle = |\bar{\varphi}\rangle = \alpha_R|0\rangle + \beta_R|1\rangle + \alpha_I|2\rangle + \beta_I|3\rangle \quad (1)$$

on some 4-level quantum system, where $\alpha = \alpha_R + i\alpha_I$ and $\beta = \beta_R + i\beta_I$, and $|n\rangle = 0, 1, 2, 3$ denotes some orthogonal basis. The action of the UNOT gate can then be simulated by a suitable unitary operator on the 4-level system.

3.3. Experimental realization

We use a trapped $^{171}\text{Yb}^+$ ion in a harmonic potential [11]. Spin B is encoded within the ground and first excited external motional states of the ion, denoted $|0\rangle_B$ and $|1\rangle_B$. Meanwhile spin A is encoded within the four internal degrees of freedom of the trapped ion using the aforementioned technique (see Fig. 1b). Arbitrary unitary operations on this 4-level system can be implemented via a sequence of appropriate microwave pulses [13,19]. This allows us to simulate any unitary or anti-unitary operation on spin A. In particular, we develop an explicit pulse sequence for simulating the UNOT gate as shown in Fig. 2.

To determine the classical and quantum correlations between spins, we develop an efficient tomography scheme that directly reconstructs the 4×4 density operator of the spin pair. This technique allows us to avoid reconstructing the full 8×8 density operator necessary to describe the state of the trapped ion, significantly reducing the number of necessary measurements to reach set levels of accuracy (see the [Supplementary data](#)). In addition, our approach involves synthesizing specialized interactions between the ion's internal and external degrees of freedom, different from the standard red sideband operation [20–22]. These interactions allow direct Bell-basis measurements for the encoded spin pair (see the [Supplementary data](#)).

3.4. Experimental results

We conduct two separate experimental tests. The first initializes $\rho_{\uparrow\uparrow}$, and determines how its classical and quantum correlations are affected by a UNOT operation on spin A. The second experiment repeats this process, using $\rho_{\uparrow\uparrow}$ in place of $\rho_{\uparrow\uparrow}$. In both cases, tomographic data is collected over 102,000 trials (see the [Supplementary data](#)). The experimentally reconstructed density operators agree with the theoretical predictions to high fidelity (see Fig. 3).

The experimentally observed effects of the UNOT gate on classical and quantum correlations are illustrated in Fig. 4. They confirm that the amount of classical correlations between A and B are preserved, in agreement with result (i). Meanwhile the application of

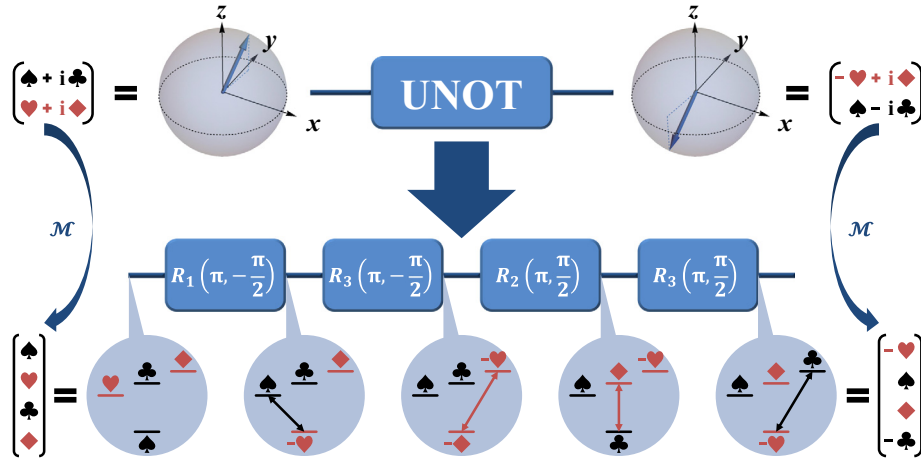


Fig. 2. Simulation of UNOT Gate on encoded spin A. While the UNOT gate is unphysical, it can be exactly simulated using a quantum 4-level system. To simulate UNOT acting on state $|\varphi\rangle = \alpha|\uparrow\rangle + \beta|\downarrow\rangle$, we initialize a suitable state $|\bar{\varphi}\rangle = \mathcal{M}|\varphi\rangle$ on the 4-level system (see Eq. (1)). The expected output state $|\varphi^{\pm}\rangle = \Theta_{\text{UNOT}}|\varphi\rangle = -\beta|\uparrow\rangle + \alpha|\downarrow\rangle$ can then be simulated by applying $\Theta_{\text{UNOT}} = |1\rangle\langle 0| - |0\rangle\langle 1| - |3\rangle\langle 2| + |2\rangle\langle 3|$ on $|\bar{\varphi}\rangle$. It is easy to check that $\Theta_{\text{UNOT}}|\bar{\varphi}\rangle = \mathcal{M}|\varphi^{\pm}\rangle$. In the ion trap system, Θ_{UNOT} can be realized with 4 microwave pulses, where $R_n(\pi, \phi) = -i(e^{-i\phi}|n\rangle_A \langle 0|_A + \text{h.c.}) + \sum_{m \neq 0,n} |m\rangle_A \langle m|_A$, $n = 1, 2, 3$.

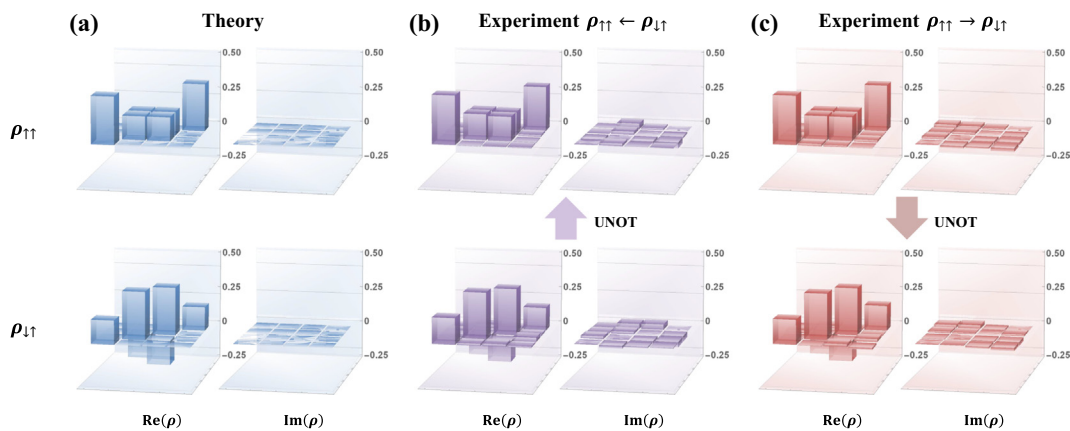


Fig. 3. Experimentally measured density operators compared with theoretical predictions. (a) illustrates the theoretically predicted density operators for $\rho_{\uparrow\uparrow}$ and $\rho_{\downarrow\downarrow}$, where each vertical bar represents a corresponding matrix element. In the first experiment (b), $\rho_{\downarrow\downarrow}$ is prepared with a fidelity of 0.992 ± 0.004 . After simulating the UNOT gate, we retrieve $\rho_{\uparrow\uparrow}$ with fidelity of 0.997 ± 0.007 . In the second experiment (c), $\rho_{\uparrow\uparrow}$ is prepared with fidelity 0.998 ± 0.004 , and the final state approximates $\rho_{\downarrow\downarrow}$ to fidelity 0.997 ± 0.002 . The errors are estimated by Monte Carlo methods with a confidence level of 95%.

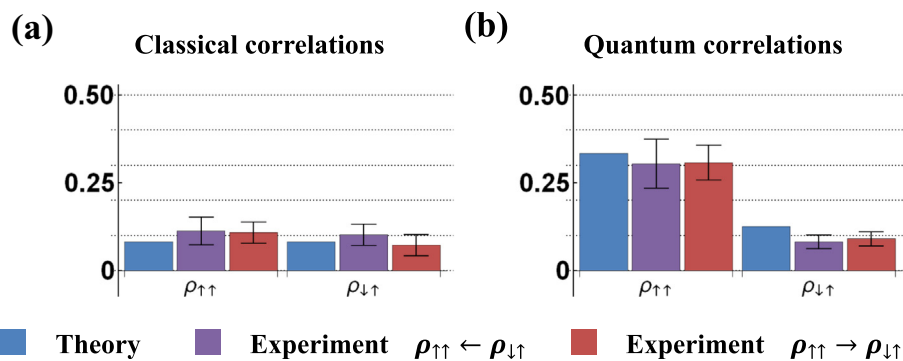


Fig. 4. The effect of UNOT gate on various types of correlations. The theoretically predicted effect of UNOT gate (blue bars), together with experimentally measured effects when acting on $\rho_{\downarrow\downarrow}$ (purple bars) and $\rho_{\uparrow\uparrow}$ (red bars) are displayed for (a) classical correlations $J(B|A)$ and (b) quantum correlations $\delta(B|A)$. (a) Theory predicts that $J(B|A) = 0.082$ for both $\rho_{\uparrow\uparrow}$ and $\rho_{\downarrow\downarrow}$. Experimental results agree within experimental error. (b) Theory predicts that $\delta(B|A)$ is 0.333 for $\rho_{\uparrow\uparrow}$ and 0.126 for $\rho_{\downarrow\downarrow}$ – a difference of 0.207. This agrees with the experiment, where we see respective increase and decrease of 0.22 ± 0.07 and 0.22 ± 0.05 when converting to and from $\rho_{\uparrow\uparrow}$.

UNOT on $\rho_{\uparrow\uparrow}$ increases quantum correlations by 0.22 ± 0.07 , violating the data processing inequality by over 5 standard deviations and thus establishing (iii). The application of the UNOT gate on $\rho_{\uparrow\uparrow}$ can reverse this, inducing a decrease in $\delta(B|A)$ of 0.22 ± 0.05 .

4. Relation to communicating with aligned vs anti-aligned spins

To conclude, we tie our results back to the communication advantage of using anti-aligned versus aligned spin pairs [1]. Specifically, consider the scenario where Alice encodes a classical message into two aligned spins, using the six possible codewords $\{|\vec{n}\rangle_A|\vec{n}\rangle_B\}_{\vec{n} \in \mathcal{E}}$ with equiprobability. The communication capacity is given by the Holevo quantity $\chi_{\uparrow\uparrow} = S(\rho_{\uparrow\uparrow})$, which bounds the amount of information Alice can communicate per spin pair [23]. This bound can always be saturated in the independent and identically distributed (i.i.d) limit, but never exceeded by conventional means.

Bob, however, can use a UNOT gate to surpass this bound. The rationale being that the capacity of such a channel $\chi_{\uparrow\uparrow} = S(A) + S(B) - I(A, B)$ can be divided into $S(A) + S(B)$, representing the amount of information A and B each individually communicate discounting correlations; and $I(A, B)$, a correction term that captures how much of the aforementioned information is redundant. $I(A, B) = J(B|A) + \delta(B|A)$ can then be further divided into classical and quantum components. The UNOT gate, acting on $\rho_{\uparrow\uparrow}$, can uniquely reduce $\delta(B|A)$, and thus reduce redundant information about \vec{n} encoded in the two spins. The UNOT gate thereby boosts the amount of information Bob can extract. The performance gain is given by $\Delta\chi = \delta_{\uparrow\uparrow}(B|A) - \delta_{\uparrow\uparrow}(B|A) \approx 0.21$, where $\delta_{\uparrow\uparrow}$ and $\delta_{\downarrow\downarrow}$ respectively represent the discord of $\rho_{\uparrow\uparrow}$ and $\rho_{\downarrow\downarrow}$. This gain exactly coincides with the change in discord.

Observe also that Bob's application of the UNOT gate is functionally equivalent to Alice encoding the message in anti-aligned spins, i.e., using the codewords $\{|-\vec{n}\rangle_A|\vec{n}\rangle_B\}_{\vec{n} \in \mathcal{E}}$ in place of $\{|\vec{n}\rangle_A|\vec{n}\rangle_B\}_{\vec{n} \in \mathcal{E}}$. Thus, we see that the performance advantage of having UNOT gates exactly coincides with the performance discrepancy between using aligned vs. anti-aligned spins. Note also that this advantage only exists assuming Bob can measure in an entangling basis. This corroborates recent evidence that many operational effects of discord can only be accessed via entangling measurements [10,24,25]. That is, the UNOT only imparts unphysical effects on the quantum component of the correlations between two spins.

5. Discussion and conclusion

This article explores the UNOT gate's capacity to locally increase the correlations between spins, and thus break the data processing inequality. We establish that this gate shows no such capability in classical domain. It obeys the data processing inequality for all classically correlated systems. Furthermore, it preserves all classical correlations within general correlated quantum systems. Violation can only be witnessed when quantum correlations are explicitly considered. We adopt state of the art techniques for simulating anti-unitary operations to experimentally demonstrate this phenomena using a trapped $^{171}\text{Yb}^+$ ion. A violation of the data processing inequality by over 5 standard deviations is observed. These results connect the unphysicality of the UNOT gate, its effect on quantum correlations, and the discrepancy in communicating using aligned versus anti-aligned spins. Our experiment then highlights how such unphysical effects can be simulated using present day ion trap technology.

There are a number of directions in which these results can generalize. Observe that the UNOT gate is equivalent, up to local uni-

tary rotation, to any other anti-unitary operator on a qubit. The effect of UNOT gates on classical and quantum correlations thus also applies to any other anti-unitary operation. Meanwhile we may extend these ideas to systems of higher dimensions. For example, in optical systems, one can communicate more information using a conjugate pair of coherent states than using the same state twice [26]. This performance difference is likely due to an analogous effect of anti-unitary operations on bipartite Gaussian correlations.

Our results could also offer a new way to capture what classes of correlations are quantum. One could take as an axiom that states whose correlations change under the UNOT gate are quantum. The motivation being such effects field no classical explanation. Such an axiom would identify certain discordant states such as $\rho = (|\vec{x}, \vec{x}\rangle|\vec{x}, \vec{x}\rangle + |\vec{z}, \vec{z}\rangle|\vec{z}, \vec{z}\rangle)/2$ as more classical than others, since we can replicate the effect of a UNOT gate acting on them using only local unitary operations. This could well generalize to multipartite systems, and present a general operational criterion for identifying quantum correlations residing somewhere between discord and entanglement.

Conflict of interest

The authors declare that they have no conflict of interest.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at <https://doi.org/10.1016/j.scib.2018.05.011>.

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